

Degradation Kinetics on the Next Level

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Main Conclusion:

Simultaneous evaluation of all datasets obtained in the same environmental medium has the potential to yield more realistic endpoints in less time.

Overview

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Degradation
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Current Guidance

Simultaneous
Evaluations

Synthetic Data

SFO
DFOP-SFO

Observed Data

Conclusions

- Current guidance
- Simultaneous evaluations
- Tests with synthetic data
- Tests with observed data
- Conclusions

Critical points regarding the FOCUS degradation kinetic guidance

Workload:

Model selection required for every dataset, and for several regulatory purposes

Ambiguities:

Expert judgement required for model selection, outcome often unpredictable

Scientific Basis:

The default half-life of 1000 days is arbitrary

State of the Art: Generalised Nonlinear Regression

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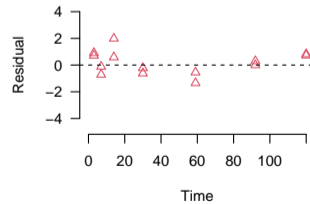
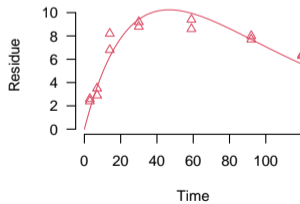
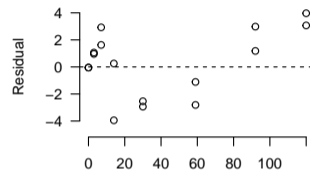
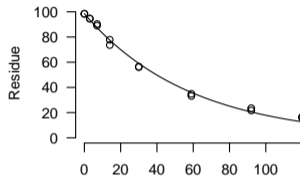
Observed Data

Conclusions

Degradation Model:
SFO-SFO

Error Model:
Constant variance

Method:
Least squares



State of the Art: Generalised Nonlinear Regression

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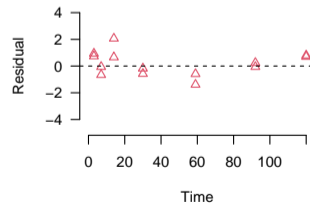
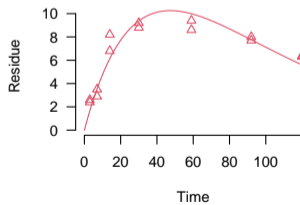
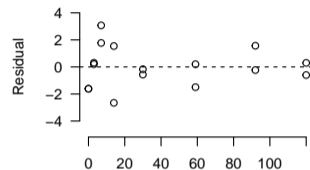
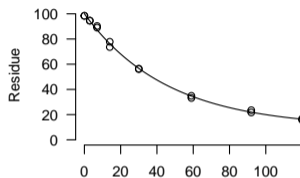
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State of the Art: Generalised Nonlinear Regression

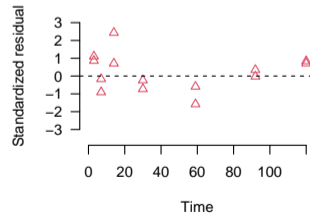
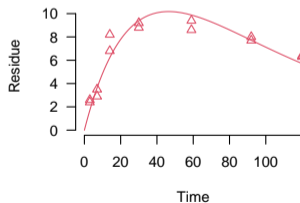
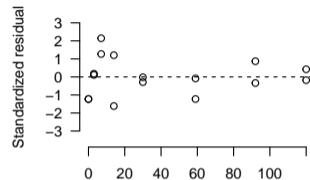
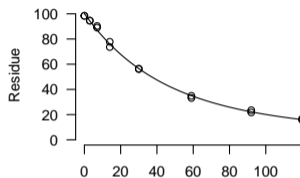
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Degradation Model:
DFOP-SFO

Error Model:
Variance by variable

Method:
Iterative reweighting
(IRLS)



State of the Art: Generalised Nonlinear Regression

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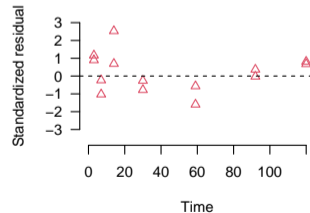
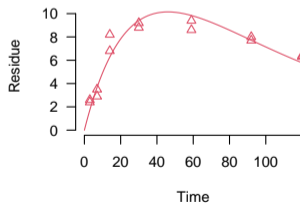
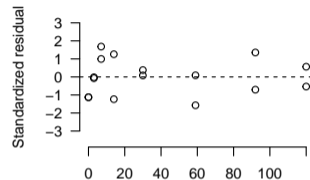
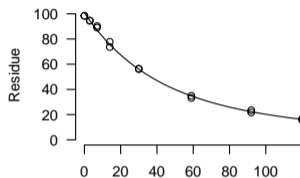
Observed Data

Conclusions

Degradation Model:
DFOP-SFO

Error Model:
Two-component

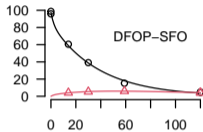
Method:
Likelihood maximisation



Separate Evaluations

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→ $n_{0,1}, k_{1,1}, k_{2,1}, \dots$

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Current Guidance

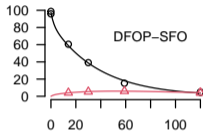
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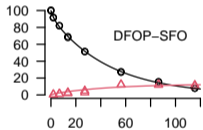
SFO
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Observed Data

Conclusions



→ $n_{0,1}, k_{1,1}, k_{2,1}, \dots$



→ $n_{0,2}, k_{1,2}, k_{2,2}, \dots$

Separate Evaluations

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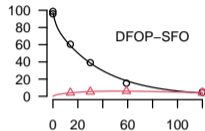
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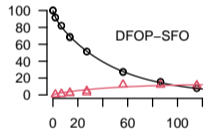
SFO
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Observed Data

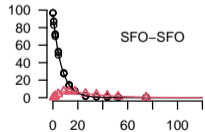
Conclusions



$\rightarrow n_{0,1}, k_{1,1}, k_{2,1}, \dots$



$\rightarrow n_{0,2}, k_{1,2}, k_{2,2}, \dots$



$\rightarrow n_{0,3}, k_3, \dots$

Separate Evaluations

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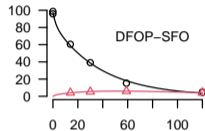
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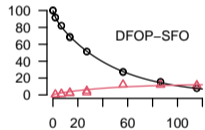
SFO
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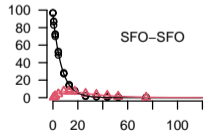
→ $n_{0,1}, k_{1,1}, k_{2,1}, \dots$



→ $n_{0,2}, k_{1,2}, k_{2,2}, \dots$

→

Geometric mean k
Mean formation fractions



→ $n_{0,3}, k_3, \dots$

The Next Level: Parameter Distribution Model

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Already Used:
Normal distribution of log rate constants

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Already Used:

Normal distribution of log rate constants

Generalised Assumption:

Suitably transformed degradation model parameters follow a normal distribution

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Already Used:

Normal distribution of log rate constants

Generalised Assumption:

Suitably transformed degradation model parameters follow a normal distribution

Well-established Method:

Nonlinear mixed-effects models for grouped data

Pinheiro and Bates (2000), Lavielle (2015)

jrwb.de

The Next Level: Parameter Distribution Model

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Already Used:

Normal distribution of log rate constants

Generalised Assumption:

Suitably transformed degradation model parameters follow a normal distribution

Well-established Method:

Nonlinear mixed-effects models for grouped data

Also known as hierarchical models or multilevel models

Simultaneous Evaluations: Nonlinear Mixed-Effects Models

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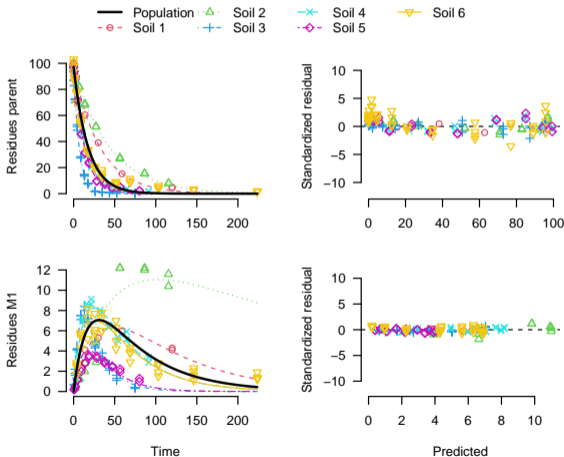
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Degradation Model:
SFO-SFO

Parameter Model:
Uncorrelated normal distribution

Error Model:
Constant variance

AIC: 1333.9 BIC: 1332.0

Simultaneous Evaluations: Nonlinear Mixed-Effects Models

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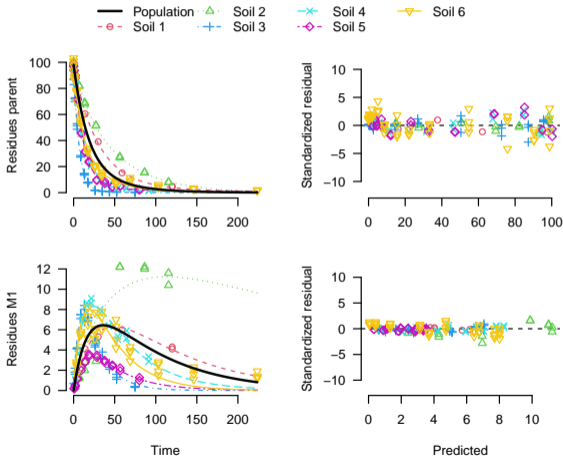
Current Guidance

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Degradation Model:
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Uncorrelated normal distribution

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Constant variance

AIC: 1185.8 BIC: 1183.1

Simultaneous Evaluations: Nonlinear Mixed-Effects Models

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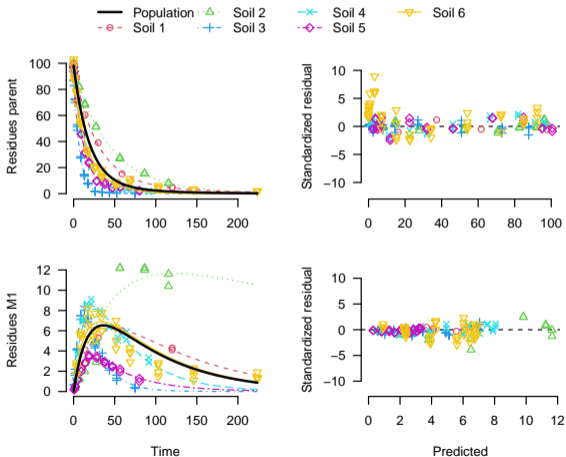
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Degradation Model:
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Parameter Model:
Uncorrelated normal distribution

Error Model:
Two-component

AIC: 1085.3 BIC: 1082.4

Simultaneous Evaluations: Nonlinear Mixed-Effects Models

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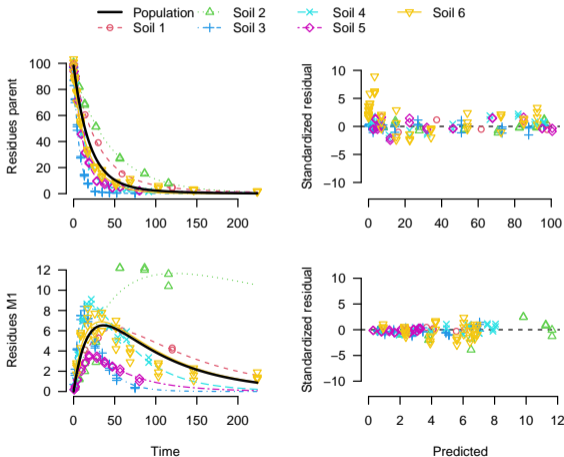
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Two-component

AIC: 1085.3 BIC: 1082.4

→ Most likely population
parameters with estimated
distributions

Recovery of Half-lives from Synthetic Data

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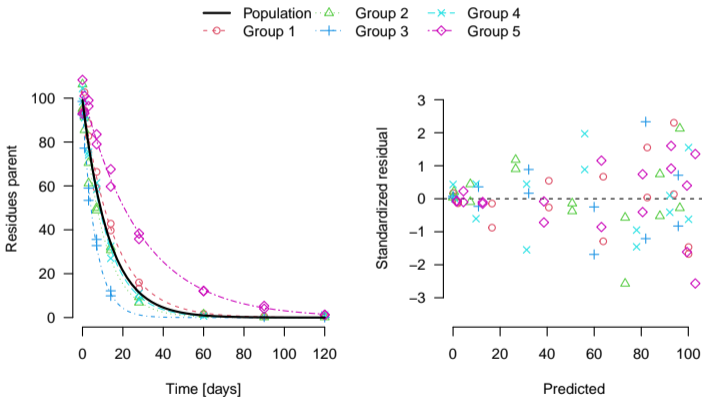
SFO
DFOP-SFO

Observed Data

Conclusions

Data Generation:
5 half-lives from
normal distribution
Two-component error
Mean DT_{50} **15 days**

Evaluation:
Separate fits
Constant variance



Recovery of Half-lives from Synthetic Data

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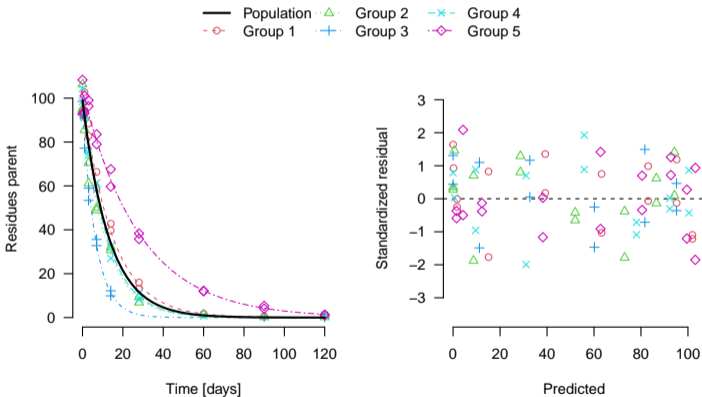
Data Generation:

5 half-lives from
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Evaluation:

Separate fits
Two-component error



Recovery of Half-lives from Synthetic Data

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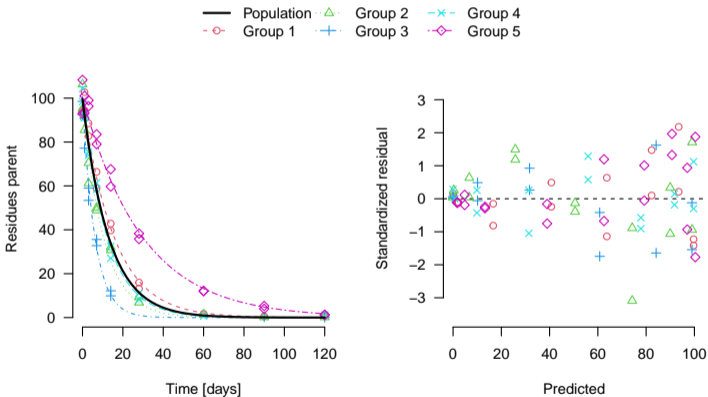
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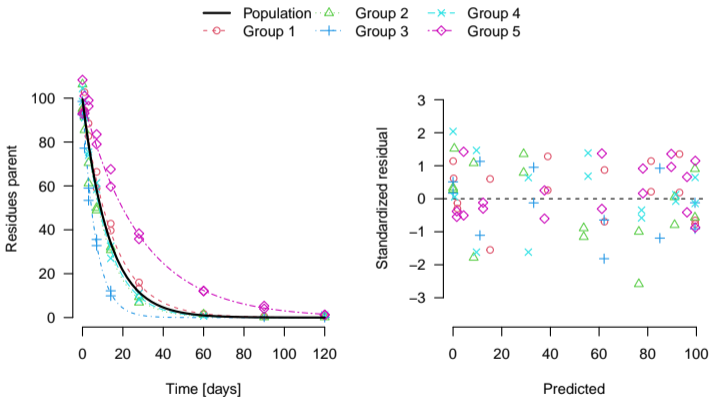
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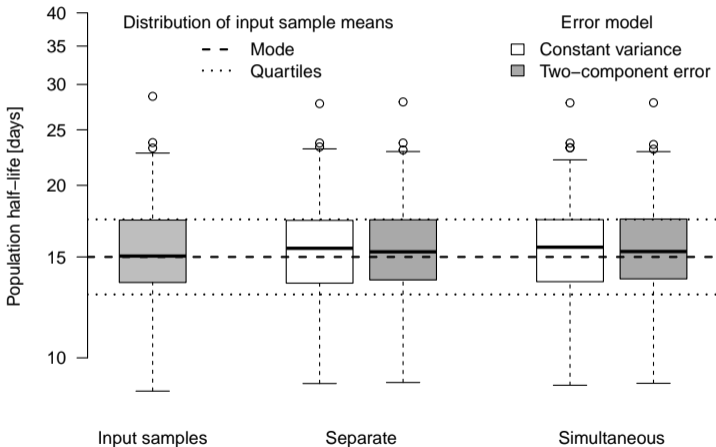
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Conclusions

Data Generation:
5 half-lives from
normal distribution
Two-component error
Mean DT_{50} **15 days**
100 x 5 datasets



Recovery of Half-lives from Synthetic Data

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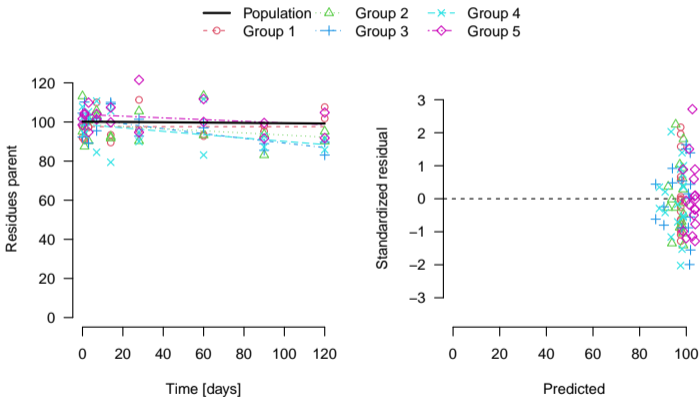
Conclusions

Data Generation:

5 half-lives from
normal distribution
Two-component error
Mean DT_{50} **800 days**

Evaluation:

Separate fits
Constant variance



Recovery of Half-lives from Synthetic Data

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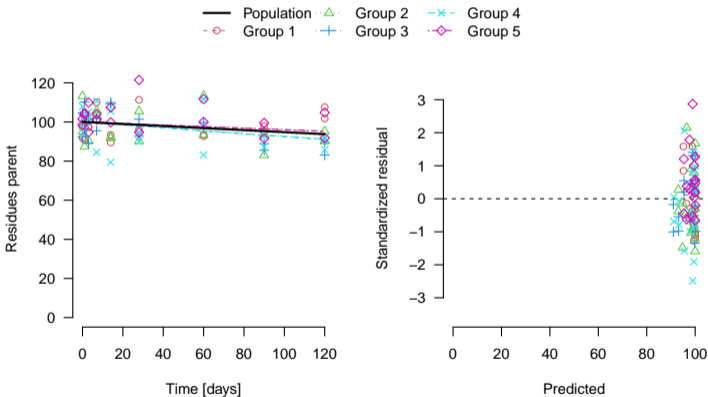
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Recovery of Half-lives from Synthetic Data

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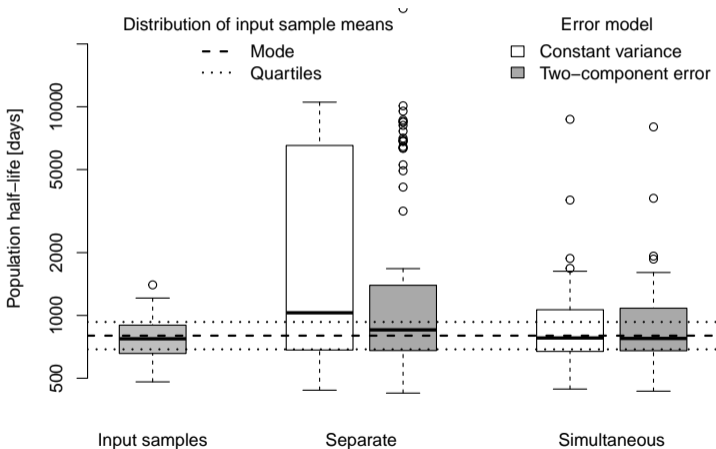
Synthetic Data
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Observed Data

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Mean DT_{50} **800 days**

Evaluation:
100 x 5 datasets



Recovery of Other Parameters from Synthetic Data

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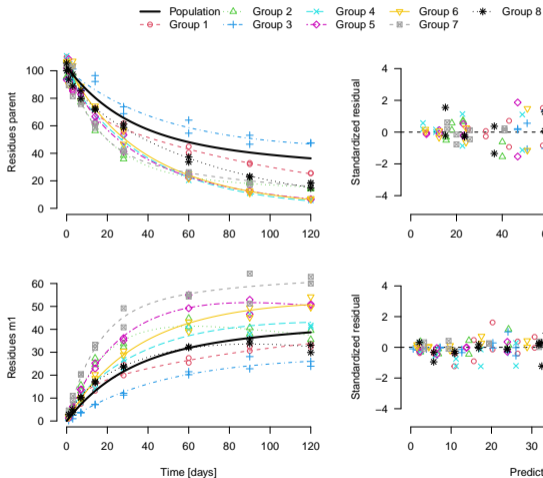
DFOP-SFO

Observed Data

Conclusions

Data Generation:
8 parameter sets from
normal distributions
of transformed parameters
Two-component error

Evaluation:
Separate fits
Constant variance



Recovery of Other Parameters from Synthetic Data

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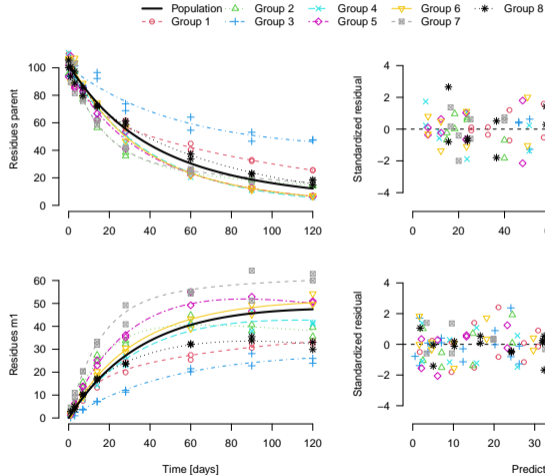
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Recovery of Other Parameters from Synthetic Data

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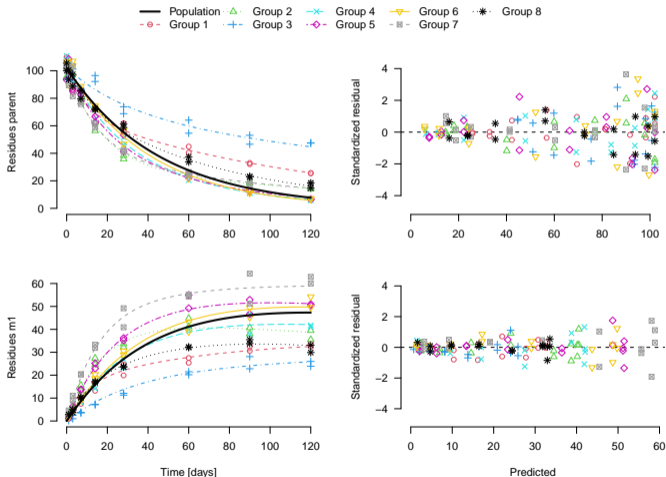
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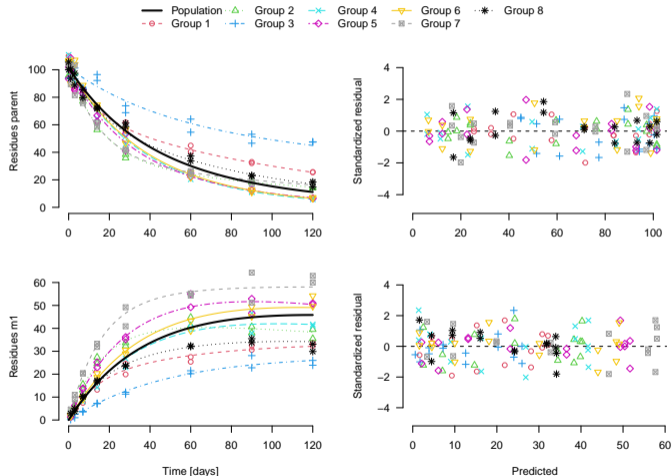
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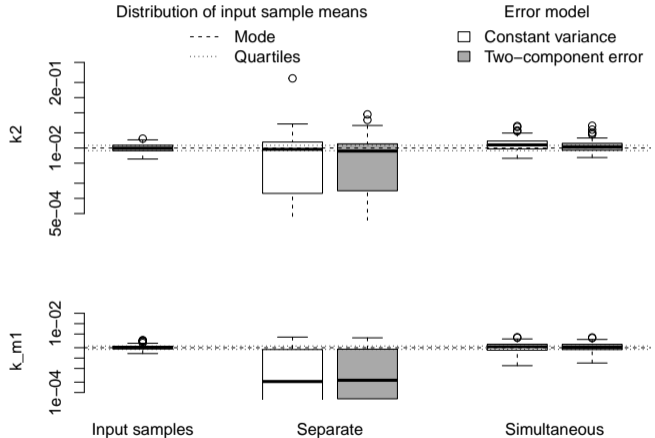
Data Generation:

8 parameter sets from
normal distributions
of transformed parameters
Two-component error

100 x 5 datasets

Critical parameters:

Slow rate constant parent
Metabolite rate constant



Recovery of Other Parameters from Synthetic Data

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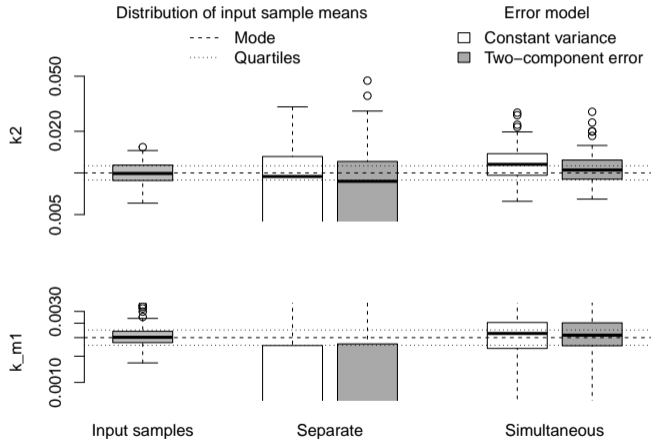
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Observed Data: Separate Evaluations

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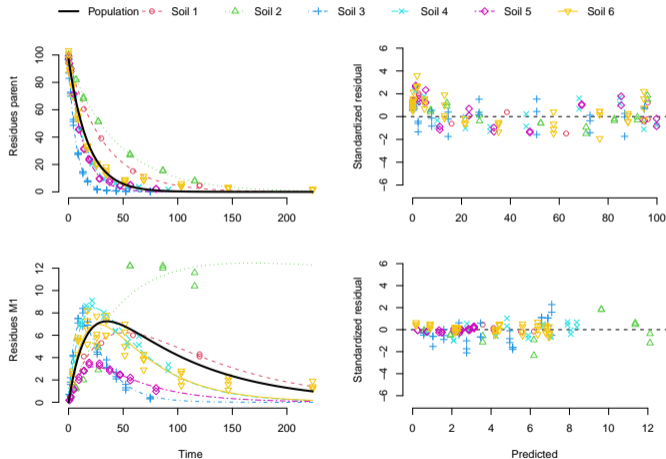
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Population Curve:
Mean values of transformed
best-fit parameters



Observed Data: Separate Evaluations

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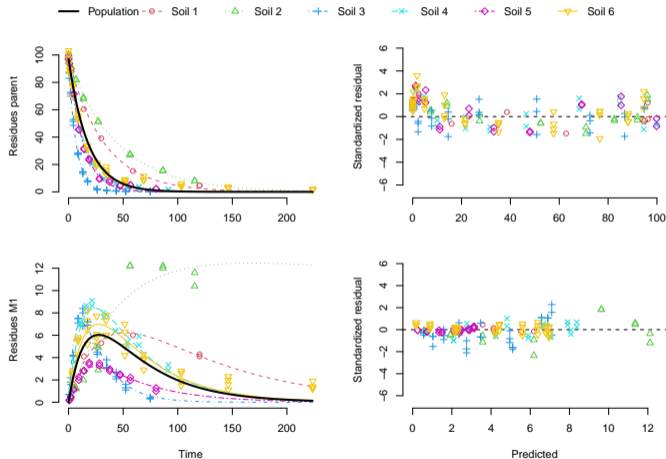
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Population Curve:
Mean values of transformed
best-fit parameters

Only significant rate
constants ($p \leq 0.10$)



Observed Data: Separate Evaluations

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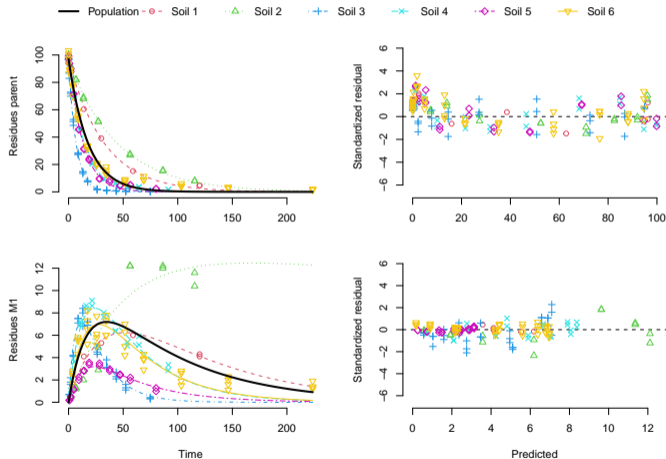
Observed Data

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Population Curve:
Mean values of transformed
best-fit parameters

Only significant rate
constants ($p \leq 0.10$)

Use default half-life of 1000
days for non-significant rate
constant (Soil 2)



Observed Data: Separate Evaluations

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Current Guidance

Simultaneous
Evaluations

Synthetic Data

SFO
DFOP-SFO

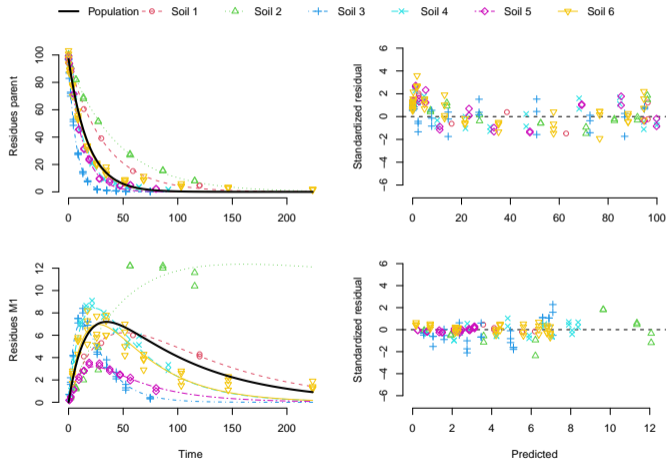
Observed Data

Conclusions

Population Curve:
Mean values of transformed
best-fit parameters

Only significant rate
constants ($p \leq 0.10$)

Use default half-life of 1000
days for non-significant rate
constant (Soil 2)
and update the formation
fraction



Observed Data: Simultaneous Evaluation

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Kinetics

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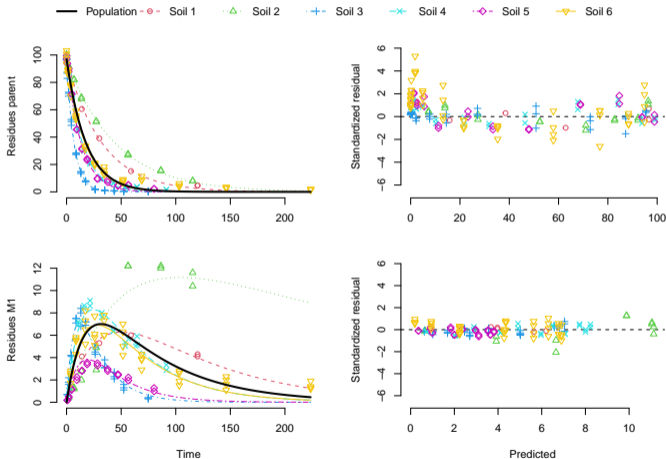
SFO
DFOP-SFO

Observed Data

Conclusions

Population Curve:
Most likely population
parameters from nonlinear
mixed-effects model

■ No data ignored



Observed Data: Simultaneous Evaluation

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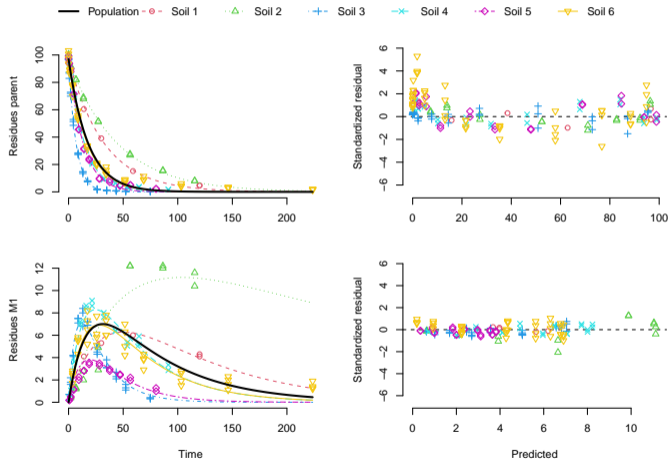
SFO
DFOP-SFO

Observed Data

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Population Curve:
Most likely population
parameters from nonlinear
mixed-effects model

- No data ignored
- No arbitrary defaults



Conclusions

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- Simultaneous evaluation of regulatory degradation data is feasible

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- Simultaneous evaluation of regulatory degradation data is feasible
- Results suggest that the method is more accurate if parameters are ill-defined in some groups

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Next Steps:

- Some technical and usability improvements are desirable
- More case studies

Acknowledgements

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